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Expanding brackets and simplifying expressions

A LEVEL LINKS

Scheme of work: 1a. Algebraic expressions - basic algebraic manipulation, indices and surds

Key points

- When you expand one set of brackets you must multiply everything inside the bracket by what is outside.
- When you expand two linear expressions, each with two terms of the form ax + b, where $a \neq 0$ and $b \neq 0$, you create four terms. Two of these can usually be simplified by collecting like terms.

Examples

Example 1 Expand 4(3x-2)

4(3x - 2) = 12x - 8	Multiply everything inside the bracket by the 4 outside the bracket
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Example 2 Expand and simplify 3(x+5) - 4(2x+3)

3(x+5) - 4(2x+3) = 3x + 15 - 8x - 12	1 Expand each set of brackets separately by multiplying $(x + 5)$ by 3 and $(2x + 3)$ by -4
= 3 - 5x	2 Simplify by collecting like terms: 3x - 8x = -5x and $15 - 12 = 3$

Example 3 Expand and simplify (x + 3)(x + 2)

(x+3)(x+2) = x(x+2) + 3(x+2)	1 Expand the brackets by multiplying $(x + 2)$ by x and $(x + 2)$ by 3
$= x^{2} + 2x + 3x + 6$	2 Simplify by collecting like terms:
= x ² + 5x + 6	2x + 3x = 5x

Example 4 Expand and simplify (x - 5)(2x + 3)

(x-5)(2x+3) = x(2x+3) - 5(2x+3)	1 Expand the brackets by multiplying $(2x + 3)$ by x and $(2x + 3)$ by -5
$= 2x^{2} + 3x - 10x - 15$ $= 2x^{2} - 7x - 15$	2 Simplify by collecting like terms: 3x - 10x = -7x



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Practice

			-	
1	Expand.			Watch out!
	a $3(2x-1)$	b	$-2(5pq + 4q^2)$	When multiplying (or
	c $-(3xy-2y^2)$			When multiplying (or dividing) positive and
2	Engend and simplify			negative numbers, if
2	Expand and simplify. $7(2 + 5) + 6(2 - 3)$	L	9(5 - 2) - 2(4 + 0)	the signs are the same
	a $7(3x+5)+6(2x-8)$		8(5p-2) - 3(4p+9) 2(4x-3) - (3x+5)	the answer is '+'; if the
	c $9(3s+1)-5(6s-10)$	a	2(4x-3) - (3x+3)	signs are different the
3	Expand			answer is '-'.
3	Expand. a $3x(4x+8)$	h	$4k(5k^2-12)$	
	a $3x(4x+8)$ c $-2h(6h^2+11h-5)$		$-3s(4s^2 - 7s + 2)$	
	c = -2n(6n + 11n - 3)	a	-55(45 - 75 + 2)	
4	Expand and simplify.			
•	a $3(y^2 - 8) - 4(y^2 - 5)$	b	2x(x+5) + 3x(x-7)	
	c $4p(2p-1) - 3p(5p-2)$		3b(4b-3) - b(6b-9)	
	P(2p 1) P(2p 2)	u		
_	$\Gamma_{\text{max}} = \frac{1}{2} \left(2 - 2 \right)$			
5	Expand $\frac{1}{2}(2y-8)$			
6	Expand and simplify.			
	a $13-2(m+7)$	b	$5p(p^2+6p)-9p(2p-3)$	
-				
7	The diagram shows a rectangle.	c	4 6	
	Write down an expression, in terms of a the rectangle.	<i>x</i> , 10	3x-5	
	Show that the area of the rectangle can	he w	vritten as	
	$21x^2 - 35x$			
				7x
8	Expand and simplify.			
	a $(x+4)(x+5)$	b	(x + 7)(x + 3)	
	c $(x+7)(x-2)$	d	(x+5)(x-5)	
	e $(2x+3)(x-1)$	f	(3x-2)(2x+1)	
	g $(5x-3)(2x-5)$	h	(3x-2)(7+4x)	
	i $(3x+4y)(5y+6x)$	j	$(x + 5)^2$	
	k $(2x-7)^2$	1	$(4x - 3y)^2$	
T	4			
Ex	tend			
~				
9	Expand and simplify $(x + 3)^2 + (x - 4)^2$			
10				
10	Expand and simplify.		2	

a
$$\left(x+\frac{1}{x}\right)\left(x-\frac{2}{x}\right)$$
 b $\left(x+\frac{1}{x}\right)^2$



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Answers

1	a	6x - 3	b	$-10pq - 8q^2$
	c	$-3xy + 2y^2$		
2	a	21x + 35 + 12x - 48 = 33x - 13		
	b	40p - 16 - 12p - 27 = 28p - 43		
	С		9 – 3	5
	d	8x - 6 - 3x - 5 = 5x - 11		
3		$12x^2 + 24x$		$20k^3 - 48k$
	с	$10h - 12h^3 - 22h^2$	d	$21s^2 - 21s^3 - 6s$
		2		- 2 - 1 -
4		$-y^2 - 4$		$5x^2 - 11x$
	c	$2p - 7p^2$	d	$6b^{2}$
5	v –	4		
3	<i>y</i> –	4		
6	я	-1 - 2m	h	$5p^3 + 12p^2 + 27p$
Ū	u	1 200	N,	5p + 12p + 27p
7	7x($(3x-5) = 21x^2 - 35x$		
		, ,		
8	a	$x^2 + 9x + 20$	b	$x^2 + 10x + 21$
	c	$x^2 + 5x - 14$	d	$x^2 - 25$
	e	$2x^2 + x - 3$	f	$6x^2 - x - 2$
	g	$10x^2 - 31x + 15$	h	$12x^2 + 13x - 14$
	-	$18x^2 + 39xy + 20y^2$	j	$x^2 + 10x + 25$
		$4x^2 - 28x + 49$		$16x^2 - 24xy + 9y^2$
	-			

9
$$2x^2 - 2x + 25$$

10 a
$$x^2 - 1 - \frac{2}{x^2}$$
 b $x^2 + 2 + \frac{1}{x^2}$

