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Expanding brackets and simplifying expressions

A LEVEL LINKS

Scheme of work: 1a. Algebraic expressions - basic algebraic manipulation, indices and surds

Key points

- When you expand one set of brackets you must multiply everything inside the bracket by what is outside.
- When you expand two linear expressions, each with two terms of the form ax + b, where $a \neq 0$ and $b \neq 0$, you create four terms. Two of these can usually be simplified by collecting like terms.

Examples

Example 1 Expand 4(3x-2)

4(3x - 2) = 12x - 8	Multiply everything inside the bracket by the 4 outside the bracket
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Example 2 Expand and simplify 3(x+5) - 4(2x+3)

3(x+5) - 4(2x+3) = 3x + 15 - 8x - 12	1 Expand each set of brackets separately by multiplying $(x + 5)$ by 3 and $(2x + 3)$ by -4
= 3 - 5x	2 Simplify by collecting like terms: 3x - 8x = -5x and $15 - 12 = 3$

Example 3 Expand and simplify (x + 3)(x + 2)

(x+3)(x+2) = x(x+2) + 3(x+2)	1 Expand the brackets by multiplying $(x + 2)$ by x and $(x + 2)$ by 3
$= x^{2} + 2x + 3x + 6$	2 Simplify by collecting like terms:
= x ² + 5x + 6	2x + 3x = 5x

Example 4 Expand and simplify (x - 5)(2x + 3)

(x-5)(2x+3) = x(2x+3) - 5(2x+3)	1 Expand the brackets by multiplying $(2x + 3)$ by x and $(2x + 3)$ by -5
$= 2x^{2} + 3x - 10x - 15$ $= 2x^{2} - 7x - 15$	2 Simplify by collecting like terms: 3x - 10x = -7x



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Practice

1	Exp	band.			Watch out!
	a	3(2x-1)	b	$-2(5pq+4q^2)$	When multiplying (or
	c	$-(3xy-2y^2)$			dividing) positive and
2	Exp	band and simplify.			negative numbers, if
	a	7(3x+5) + 6(2x-8)	b	8(5p-2) - 3(4p+9)	the signs are the same the answer is $(+)$ if the
	c	9(3s+1) - 5(6s-10)	d	2(4x-3) - (3x+5)	signs are different the
					answer is '-'.
3	Exp	band.		l	
	a	3x(4x+8)	b	$4k(5k^2-12)$	
	C	$-2h(6h^2+11h-5)$	d	$-3s(4s^2-7s+2)$	
4	Exp	oand and simplify.			
	a	$3(y^2 - 8) - 4(y^2 - 5)$	b	2x(x+5) + 3x(x-7)	
	c	4p(2p-1) - 3p(5p-2)	d	3b(4b-3) - b(6b-9)	
_	_	. 1			
5	Exj	pand $\frac{1}{2}(2y-8)$			
6	Exr	and and simplify.			
-	a	13 - 2(m + 7)	b	$5p(p^2+6p)-9p(2p-3)$	
7	The	e diagram shows a rectangle.			
	Wri	ite down an expression, in terms of a rectangle	x, foi	the area of $3x-5$	
	Sho	by that the area of the rectangle can	be w	ritten as	
	21x	$x^2 - 35x$	00 11		
					/X
8	Exp	band and simplify.			
	a	(x+4)(x+5)	b	(x+7)(x+3)	
	c	(x+7)(x-2)	d	(x+5)(x-5)	
	e	(2x+3)(x-1)	f	(3x-2)(2x+1)	
	g	(5x-3)(2x-5)	h	(3x-2)(7+4x)	
	i	(3x+4y)(5y+6x)	j	$(x+5)^2$	
	k	$(2x-7)^2$	1	$(4x-3y)^2$	
Ex	ten	nd			
9	Exp	band and simplify $(x + 3)^2 + (x - 4)^2$			
10	Exp	and and simplify.			

a
$$\left(x+\frac{1}{x}\right)\left(x-\frac{2}{x}\right)$$
 b $\left(x+\frac{1}{x}\right)^2$



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Answers

a	6x - 3	b	$-10pq - 8q^2$
c	$-3xy + 2y^2$		
a	21x + 35 + 12x - 48 = 33x - 13		
b	40p - 16 - 12p - 27 = 28p - 43		
c	27s + 9 - 30s + 50 = -3s + 59 = 5	9-3	S
d	8x - 6 - 3x - 5 = 5x - 11		
a	$12x^2 + 24x$	b	$20k^3 - 48k$
c	$10h - 12h^3 - 22h^2$	d	$21s^2 - 21s^3 - 6s$
a	$-y^2 - 4$	b	$5x^2 - 11x$
c	$2p - 7p^2$	d	$6b^{2}$
y –	4		
y —	4		
у — а	4 $-1 - 2m$	b	$5p^3 + 12p^2 + 27p$
у — а	4 $-1 - 2m$	b	$5p^3 + 12p^2 + 27p$
y – a 7 <i>x</i> (2	4 $-1 - 2m$ $3x - 5) = 21x^2 - 35x$	b	$5p^3 + 12p^2 + 27p$
y – a 7 <i>x</i> (2	4 $-1 - 2m$ $3x - 5) = 21x^2 - 35x$	b	$5p^3 + 12p^2 + 27p$
y – a 7x(2 a	4 $-1 - 2m$ $3x - 5) = 21x^{2} - 35x$ $x^{2} + 9x + 20$	b	$5p^3 + 12p^2 + 27p$ $x^2 + 10x + 21$
y – a 7 <i>x</i> (2 a c	4 $-1 - 2m$ $3x - 5) = 21x^{2} - 35x$ $x^{2} + 9x + 20$ $x^{2} + 5x - 14$	b b d	$5p^3 + 12p^2 + 27p$ $x^2 + 10x + 21$ $x^2 - 25$
y – a 7 <i>x</i> (2 a c e	4 -1 - 2m $3x - 5) = 21x^{2} - 35x$ $x^{2} + 9x + 20$ $x^{2} + 5x - 14$ $2x^{2} + x - 3$	b b d f	$5p^{3} + 12p^{2} + 27p$ $x^{2} + 10x + 21$ $x^{2} - 25$ $6x^{2} - x - 2$
y – a 7x(: a c e g	4 -1 - 2m $3x - 5) = 21x^{2} - 35x$ $x^{2} + 9x + 20$ $x^{2} + 5x - 14$ $2x^{2} + x - 3$ $10x^{2} - 31x + 15$	b d f h	$5p^{3} + 12p^{2} + 27p$ $x^{2} + 10x + 21$ $x^{2} - 25$ $6x^{2} - x - 2$ $12x^{2} + 13x - 14$
y - a $7x(1)$ a c g i	4 -1 - 2m $3x - 5) = 21x^{2} - 35x$ $x^{2} + 9x + 20$ $x^{2} + 5x - 14$ $2x^{2} + x - 3$ $10x^{2} - 31x + 15$ $18x^{2} + 39xy + 20y^{2}$	b d f h j	$5p^{3} + 12p^{2} + 27p$ $x^{2} + 10x + 21$ $x^{2} - 25$ $6x^{2} - x - 2$ $12x^{2} + 13x - 14$ $x^{2} + 10x + 25$
	c a b c d a c a c	c $-3xy + 2y^2$ a $21x + 35 + 12x - 48 = 33x - 13$ b $40p - 16 - 12p - 27 = 28p - 43$ c $27s + 9 - 30s + 50 = -3s + 59 = 5$ d $8x - 6 - 3x - 5 = 5x - 11$ a $12x^2 + 24x$ c $10h - 12h^3 - 22h^2$ a $-y^2 - 4$ c $2p - 7p^2$	c $-3xy + 2y^2$ a $21x + 35 + 12x - 48 = 33x - 13$ b $40p - 16 - 12p - 27 = 28p - 43$ c $27s + 9 - 30s + 50 = -3s + 59 = 59 - 3$ d $8x - 6 - 3x - 5 = 5x - 11$ a $12x^2 + 24x$ b c $10h - 12h^3 - 22h^2$ d a $-y^2 - 4$ b c $2p - 7p^2$ d

9
$$2x^2 - 2x + 25$$

10 a
$$x^2 - 1 - \frac{2}{x^2}$$
 b $x^2 + 2 + \frac{1}{x^2}$

